

# Crystal Field Handbook

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This bibliography was created in the process of writing the book. It contains many more references than appear in the final book.

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